#### FST 3-5 Notes

Topic: The Graph Scale-Change Theorem

GOAL: Apply the Graph Scale Change Theorem to all relations.

#### **SPUR Objectives**

C Use the Graph Scale-Change Theorem to find transformation images.

D Describe the effects of translations and scale changes on functions and their graphs.

J Apply the Graph-Translation Theorem or the Graph Scale-Change Theorem to make or identify graphs.

### Vocabulary

horizontal and vertical scale change scale factor size change

horizontal scale factor A transformation that maps (x, y) to (ax, y) for all (x, y), where  $a \neq 0$  is a constant.

vertical scale change A transformation that maps (x, y) to (x, by), where  $b \neq 0$  is a constant.

scale change (in the plane) A transformation that maps (x, y) to (ax, by), where  $a \neq 0$  and  $b \neq 0$  are constants.

scale factor The nonzero constant by which each data value is multiplied in a scale change.

size change A scale change in which the scale factors are equal; a transformation that maps (x, y) to (kx, ky), where k is a nonzero constant.



# - 1 y=(2x)2-4

#### **Horizontal Scale Changes**

- 1. Use your calculator to graph  $y = x^2 4$ . Sketch the graph in the space provided at the right. Be sure to label all intercepts (x and y).
- 2. Graph  $y = (2x)^2 4$  on the same set of axes.
- Q1: How did the equation change?

X multiplied by Q, then squared

- Q2: What changed in your graph? How did it change? Horizontal Shrink by à
- Q3: What stayed the same in graphs from steps 1 & 2.

Vertex (0,-4) same

- 3. Graph  $y = \left(\frac{x}{2}\right)^2 4$  on the same set of axes above.
- Q4: How did the equation change in step 3 from the original equation in step 1?

disided by 2 then Squared

- Q5: What changed in the graph? How did it change? Horizontal States of 2
- Q6: What stayed the same in all 3 graphs?

Vertex 6,-4) Same for all grans

#### Vertical Scale Changes

- 4. Graph  $y = x^2 4$  at the right again. Be sure to label all intercepts (x and y).
- 5. Graph  $2y = x^2 4$  on the same set of axes. (Hint: Solve equation for y) フ= ギーマ

Q7: How did the equation change?

Q8: What changed in your graph? How did it change?

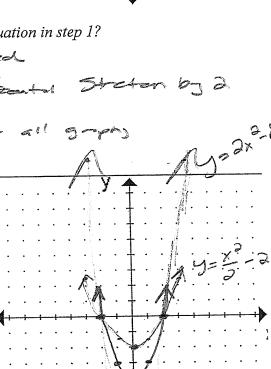
Vertical Shruk by -

Q9: What stayed the same in graphs from steps 4 & 5.

X-interests arc same

- 6. Graph  $\frac{y}{2} = x^2 4$  on the same set of axes above. (Hint: Solve equation for y)
- Q10: How did the equation change in step 6 from the original equation in step 4? multiplied by a
- Q11: What changed in the graph? How did it change? Vertee! Stretch 52
- Q12: What stayed the same in all 3 graphs?

X-interests are same



## Graph Scale-Change Rule: S(x, y) = (ax, by)

Where:

a

is the horizontal scale factor

is the vertical scale factor b

Recall

Translation Rule:  $T(x,y) \to (x+h,y+k)$ In equation form, the 'opposite' happened – addition in the translation rule corresponded to subtraction in the caustics. to subtraction in the equation

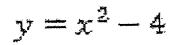
If y = f(x) was translated by the rule above, the new equation would be y - k = f(x - h)

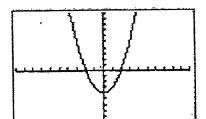
# The same 'opposite' happens between the rule for scale change and the equation

Multiplication in rule corresponds to division in equation

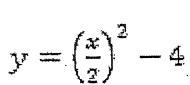
Division in rule corresponds to multiplication in equation

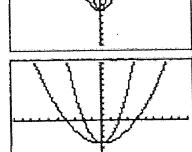
# From Activity:

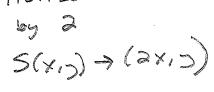


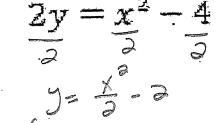


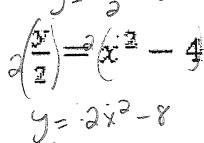
$$y = (2x)^2 - 4$$

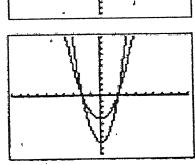








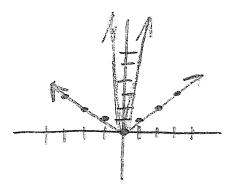




e Vertical Streton

# **Additional Example 1**

Sketch and compare the graphs of y = |x| and  $\frac{y}{4} = |6x|$ . Describe the transformation that maps the first graph onto the second.



$$\frac{9}{4} = 16x1$$
 $y = 416x1$ 

(+,45)

. Horizontal Shrink by 1/6. Oction Stretch by 4

& multiplication in rule is dissist in equation & Division in rule is multiplication in equation

# **Additional Example 2**

The line 41x - 29y = 700 contains the points (39, 31) and (10, -10). Use this information to obtain two points on the line with equation 20.5x - 87y = 700.

$$\frac{41}{3}x - (3)(39)_{3} = 700$$

$$\frac{x}{3} - 3y = 700 \rightarrow -3y = -\frac{x}{3} + 700$$

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