FST 6-1 Notes

Topic: Introduction to probability

GOAL

Introduce the basic vocabulary and principles of probability. Calculate probability for events in which the sample space is small and finite and the outcomes are equally likely.

SPUR Objectives

A Compute probabilities of events in various contexts.

G List sample spaces and events for experiments.

	Bo. C	sample space
Experiment	Sample Space	
flipping a coin	(heads, tails)	probability of an event, $P(E)$
tossing a six-sided die	{1, 2, 3, 4, 5 6}	fair, unbiased Allocation Telect
taking an antibiotic for a sore throat	{sore throat cured, sore throat continues}	randomly, at random
picking an integer from 1 to 100	$\{n \in \mathbb{Z} \mid 1 \le n \le 100\}$	empty set, null set 130 ELEASTS

Vocabulary

- outcome

probability theory 50-07 OF CHARLE

WARM UP

A drawer contains r red socks, b blue socks, and w white socks. Assume that you draw a sock randomly from the drawer.

		r
1.	What is the probability that it is red?	r+b+w

2. What is the probability that it is not red?
$$\frac{b + w}{v + b + w}$$

3. What is the probability that it is green?
$$\frac{\bigcirc}{\vee + \triangleright + \sim}$$

Term	Definition	From Warm up picking a sock from a drawer	
EXPERTMENT	A situation with several possible results		
OUTCOME	the result of an experiment	the color of sock that was picked	
SAMPLE SPACE	set of all possible outcomes	all the socks in the drawer	
EVE	desired outcome, subset of sample space	in part a, the event was a red sock	

Example 1: A small box contains 30 blue, 30 green, and 25 red paper clips. Two paper clips are taken from the box and their colors are recorded.

a) List all possible outcomes for this experiment.

86 66 FR 86 68

BR

b) How many outcomes are in the sample space for this experiment?

6

Example 2: Two fair dice are rolled, both 6-sided.

a) What are all the possible outcomes? = 36

	1		3			
1	1,1	1,2	1,3	1,4	01,5	11,0
	1		3	š .	ĸ	26
3	3,1	3,2	3,3	34	3,5	3,5
4	4,6	$\dot{\mu}_i \supset$	4,3	4.9	4,5	4.4
5	5	5,2	53	54	5.5	5,6
						4,4

b) List the outcomes if the event is a sum of the number is 5.

c) Give the probability that the sum of the numbers is 5.

The probability of an event is a number from 0 to 1 that measures the likelihood or chance that the event will occur. It can be written as a fraction, decimal or percent.

"Equally likely" means each outcome has an equal chance of happening.

	м,			*
P=0	P = 0.25	P = 0.5	P = 0.75	P = 1
Impossible	Unlikely	Equally likely to	Likely	Certain
		occur or not occur		

Let E be an event in a finite sample space S. Let N(E) and N(S) be the numbers of elements in E and S, respectively. If each outcome in S is equally likely, then the probability that E occurs, called the **probability** of E and denoted P(E), is given by

$$P(E) = \frac{N(E)}{N(S)} = \frac{\text{number of outcomes in event}}{\text{number of outcomes in the sample space}}$$

prob = # desired outcomes # possible outcomes

Example 3: In the situation of Example 1, which of the six outcomes are equally likely?

What are their probabilities?

What are their probabilities?

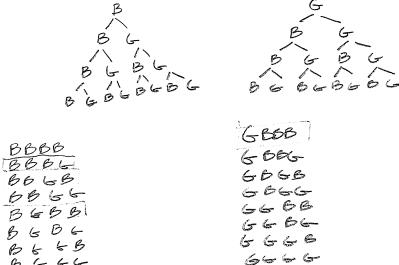
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$$\left(\frac{30}{85}\right)\left(\frac{29}{84}\right) = \frac{870}{7140}$$

$$BG\left(\frac{39}{85}\right)\left(\frac{39}{84}\right) = \frac{900}{7140}$$

BK
$$\left(\frac{3}{85}\right)\left(\frac{25}{84}\right) = \frac{750}{7140}$$

Example 4: Assume that births of boys and girls are equally likely. A family has 4 children.

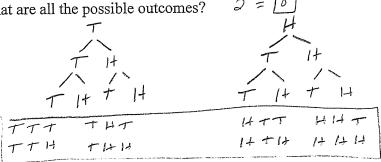
a) How many outcomes are in the same sample space? List the outcomes.



b) Find the probability that a family of 4 children has one girl and three boys.

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Example 5: Three fair coins are flipped.



b) List the outcomes if the event is 1 tails and 2 heads.

$$THH$$
, HTH , $HHT = 3$

c) Give the probability for the event in part (b).

If an event contains no possible outcomes, then it cannot occur and it has probability of 0. A set with no elements is called the empty set or the null set and is denoted either by the symbol $\{ \}$ or \emptyset . $P(\{ \})$ or $P(\emptyset) = 0$.

If an event is certain to happen, then it contains all the possible outcomes in the sample

space, and has probability 1.
$$N(E) = N(S)$$
, so $P(E) = \frac{N(E)}{N(S)} = 1$.

Let S be the sample space associated with an experiment. Then, for any outcome or event E in S.

(i)
$$0 \le P(E) \le 1$$
.

(ii) if
$$E = S$$
, then $P(E) = 1$.

(iii) if
$$E = \emptyset$$
, then $P(E) = 0$.

Relative Frequencies and Probabilities

- They are related, but their meanings differ
- Both have values that range from 0 to 1
- A relative frequency of 0 means the event has not occurred, but this does not guarantee that the probability is 0 (same if relative frequency is 1)
- However, if probability of an event is 0, then the relative frequency is also 0 (same if probability is 1)