#### FST 6-3 Notes

Topic: Counting Strings with Replacement

**GOAL** 

Apply the Multiplication Counting Principle to intuit the formulas for the number of strings with replacement of length k and a set S with n elements.

#### SPUR Objectives

B Find the number of strings with replacement.

E Determine whether events are independent or dependent.

I Calculate probabilities in real situations.

J Use the Multiplication Counting Principle and the Strings with Replacement Theorem to find the number of ways of arranging objects.

### Vocabulary

string

length of a string

independents events

dependent events

Write down all the three-letter combinations that begin with D using the letters:

A, B, C, D, and E only once.

DAG DBA DCA DEA DAC DGC DCB DEB DAE DBE DCE DEG must A,B,C,E Thee Combinations
be less
"0"

the remain
from choice for

and letter

How many three-letter combinations are there using the letters: A, B, C, D, and E only once?

5. 4. 3 = 60 continuation

### **Multiplication Counting Principle Review**

You have 4 different colored socks, 5 different colored pants, and 3 different colored shirts. How many combinations can you make?

5 = 60 Sacks Party Shrips out-lits

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Let A and B be any finite sets. The number of ways to choose one element from A and then one element from B is  $N(A) \cdot N(B)$ .

Example 1: A lottery game played in some states involves picking 3 digits from 0 to 9 in order. Describe a sample space for this experiment and determine the number of elements in the sample space.

Sample Spriz: 500 - 979

# of zlamonts in Sample Spriz: 10.10.10

= 1000

When symbols (numbers, objects, etc...) in a problem must be <u>ordered</u>, the ordered list is a **string**.

The number of symbols in the sting is its length.

string: do not think of cord or wire, instead think of a "string of pearls" where a group of objects are arranged one after the next



**Example 2:** Three of the questions on a science test are multiple choice with four choices each.

a) How many ways are there to answer these questions?

$$\frac{4}{Q_1}$$
,  $\frac{4}{Q_2}$ ,  $\frac{4}{Q_3}$  =  $4^3 = 64$ 

b) If you guess randomly on each of these questions, what is the probability of answering all these correctly?

$$(4)(4)(4) = (4)^3 = \frac{1}{64} = 0.015625$$

The previous problem was an example of strings with replacement – symbols can be used over and over again.

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Let S be a set with n elements. Then there are  $n^k$  possible strings with replacement of length k with elements from S.

Example 3: Some states allow license plates with 3 letters followed by 4 digits from 0 through 9. How many license plates are possible?

Selections with replacement are independent events.

For example: In the previous problem the second letter did not depend upon what the first letter was.

Independent event problems use the Multiplication Counting Principle to find probability.

# Events A and B are **Independent events** if and only if $P(A \cap B) = P(A) \cdot P(B)$ .

Events that are not independent are called **dependent events**.

**Example 4:** In a certain spinning wheel, there are 20 sectors of equal size. In 18 of these sectors, you win a prize, but in the other 2, you lose all your winnings. If the wheel spins randomly, what is the probability of winning five prizes and then losing on the sixth spin?

$$\frac{18}{20} = \frac{18}{20} = \frac{18$$