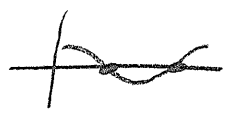


③ $y = \cos(x + \frac{\pi}{2}) \quad -\frac{\pi}{2} \leq x \leq \frac{3\pi}{2}$



$x + \frac{\pi}{2} = 0$

$x + \frac{\pi}{2} = 2\pi$

Amplitude = 1

$x = -\frac{\pi}{2}$

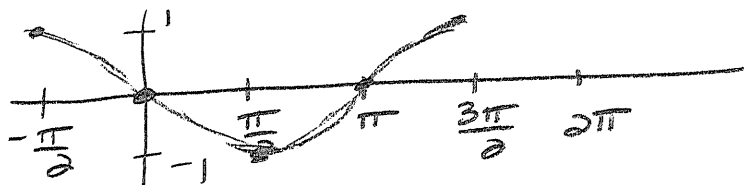
$x = \frac{3\pi}{2}$

Period = 2π

Start

End

P.S. = $-\frac{\pi}{2}$



⑥ $y = \cos(x + \frac{\pi}{4}) \quad -\pi \leq x \leq 2\pi$

$x + \frac{\pi}{4} = 0$

$x + \frac{\pi}{4} = 2\pi$

Amplitude = 1

$x = -\frac{\pi}{4}$

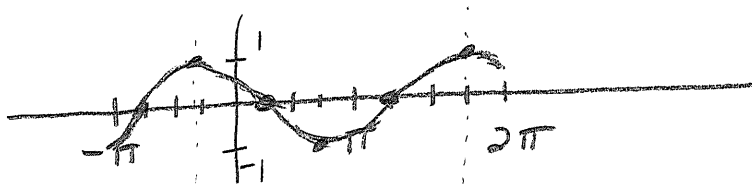
$x = 1\frac{3}{4}\pi$ or $\frac{7\pi}{4}$

Period = 2π

Start

End

P.S. = $-\frac{\pi}{4}$



⑨ $y = -2 \cos(2x + \pi) \quad -\pi \leq x \leq 3\pi$

$2x + \pi = 0$
 $-\pi \quad -\pi$

$2x + \pi = 2\pi$
 $-\pi \quad -\pi$

Amplitude = 2

★ FLIP ★

$\frac{2x}{2} = \frac{-\pi}{2}$

$\frac{2x}{2} = \frac{\pi}{2}$

Period = $\frac{2\pi}{2} = \pi$

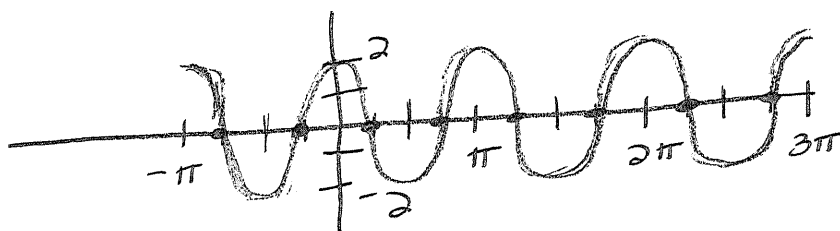
$x = -\frac{\pi}{2}$

$x = \frac{\pi}{2}$

P.S. = $-\frac{\pi}{2}$

Start

End

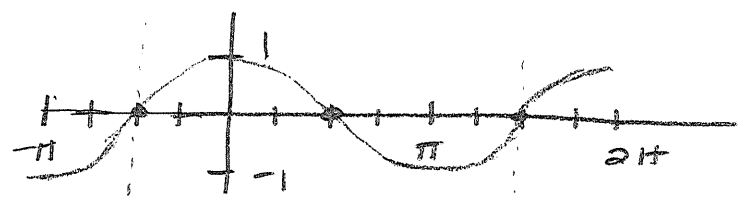


12) $y = \sin(x + \frac{\pi}{2})$ $y = \cos x$

$x + \frac{\pi}{2} = 0$ $x + \frac{\pi}{2} = 2\pi$
 $-\frac{\pi}{2} - \frac{\pi}{2}$ $x = \frac{3\pi}{2}$
 $x = -\frac{\pi}{2}$ End
 Start

★ They produce SAME Graph. ★

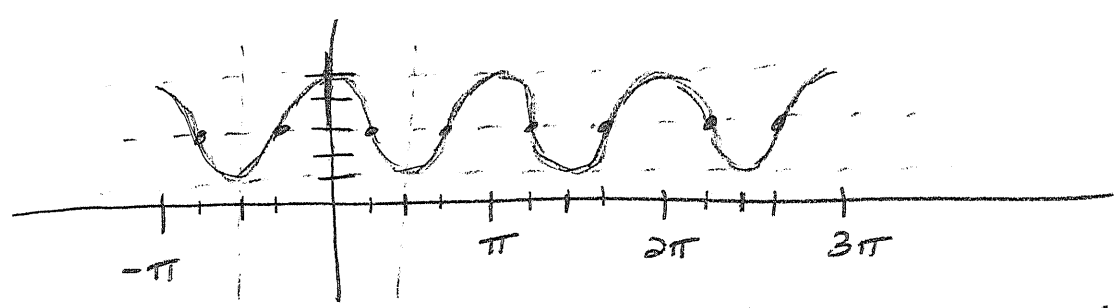
Amp = 1 Period = 2π P.S. = $-\frac{\pi}{2}$



15) $y = 3 - 2 \cos(2x + \pi)$ $-\pi \leq x \leq 3\pi$

↑ 3 Amp = 2 ★ FLIP ★ Period = $\frac{2\pi}{2} = \pi$

$2x + \pi = 0$ $2x + \pi = 2\pi$
 $-\pi - \pi$ $-\pi - \pi$
 $\frac{2x}{2} = \frac{-\pi}{2}$ $\frac{2x}{2} = \frac{\pi}{2}$
 $x = -\frac{\pi}{2}$ $x = \frac{\pi}{2}$
 Start End



17) $y = 2 \sin(\pi x - \frac{\pi}{2})$ [B]

Amp = 2 P = $\frac{2\pi}{\pi} = 2$
 $\pi x - \frac{\pi}{2} = 0$ $\pi x - \frac{\pi}{2} = 2\pi$
 $\frac{\pi x}{\pi} = \frac{\pi}{\pi}$ $\frac{\pi x}{\pi} = \frac{5\pi}{\pi}$
 $x = \frac{1}{2}$ $x = \frac{5}{2}$
 Start End
 P.S. = $\frac{1}{2}$

18) $y = 2 \cos(\pi x + \frac{\pi}{2})$ [C]

Amp = 2 P = $\frac{2\pi}{\pi} = 2$
 $\pi x + \frac{\pi}{2} = 0$ $\pi x + \frac{\pi}{2} = 2\pi$
 $\frac{\pi x}{\pi} = \frac{-\pi}{\pi}$ $\frac{\pi x}{\pi} = \frac{5\pi}{\pi}$
 $x = -\frac{1}{2}$ $x = \frac{5}{2}$
 Start End
 P.S. = $-\frac{1}{2}$

$$(19) y = 2 \cos\left(2x + \frac{\pi}{2}\right) \quad \boxed{A}$$

$$\text{Amp} = 2 \quad P = \frac{2\pi}{2} = \pi$$

$$2x + \frac{\pi}{2} = 0$$

$$\frac{2x}{2} = \frac{-\frac{\pi}{2}}{2}$$

$$x = -\frac{\pi}{4}$$

$$2x + \frac{\pi}{2} = 2\pi$$

$$-\frac{\pi}{2} \quad -\frac{\pi}{2}$$

$$\frac{2x}{2} = \frac{\frac{3\pi}{2}}{2}$$

$$x = \frac{3\pi}{4}$$

$$(20) y = 2 \sin\left(2x - \frac{\pi}{2}\right) \quad \boxed{D}$$

$$\text{Amp} = 2 \quad P = \frac{2\pi}{2} = \pi$$

$$2x - \frac{\pi}{2} = 0$$

$$\frac{2x}{2} = \frac{\frac{\pi}{2}}{2}$$

$$x = \frac{\pi}{4}$$

$$2x - \frac{\pi}{2} = 2\pi$$

$$\frac{2x}{2} = \frac{\frac{5\pi}{2}}{2}$$

$$x = \frac{5\pi}{4}$$